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# Lyapunov Based Control of Hybrid Energy Storage System in Electric Vehicles

H. El Fadil, F. Giri, Josep M. Guerrero

**Abstract**—This paper deals with a Lyapunov based control principle in a hybrid energy storage system for electric vehicle. The storage system consists on fuel cell (FC) as a main power source and a supercapacitor (SC) as an auxiliary power source. The power stage of energy conversion consists on a boost converter connected with the main source and a buck-boost converter connected with the auxiliary source. The converters share the same dc bus which is connected to the traction motor through an inverter. The aim is controlling power converters in order to satisfy the following requirements: i) tight dc bus voltage regulations, ii) perfect tracking of SC current to its reference, and iii) asymptotic stability of the closed loop system. It is clearly shown, using formal analysis and simulations that the designed controller meets all the objectives.

## I. INTRODUCTION

Oil crisis and environmental issues continue to worry vehicle manufacturers. Nowadays, much research has been undertaken on technologies for future vehicles. Among these technologies the hybrid electric vehicle (HEV) is an efficient and promising solution ([1], [2]). Most hybrid electric vehicle configurations use two energy storage devices: one with high energy storage capability, called "Main Energy System" (MES), and the other with high power capability and reversibility, called "Auxiliary Energy System" (AES). The MES provides extended driving range and the AES good acceleration and regenerative braking. Accordingly, Fuel cell (FC) based vehicles have the potential to improve significantly the fuel economy and can be more efficient than traditional internal combustion engines ([3], [4], [5]). The development and infrastructure of FC technologies have been advancing rapidly to improve overall system efficiency under realistic automotive loads while meeting the demands for dynamic response under transient loads or cold start conditions ([6], [7]). Although there are various FC technologies available for use in vehicular systems, according to scientists and vehicle developers, a prime candidate is the proton exchange membrane FC (PEMFC), [8], because the PEMFC has higher power density and lower operating temperatures than other types of FC systems. A stand alone FC system integrated into an automotive power train is not always sufficient to provide the load demands of a

vehicle [9]. To provide the initial peak power during transients such as start up, acceleration or sudden changes in load and also to take advantage of the regenerative power of an electric vehicle at braking, a supercapacitor (SC) bank is needed in addition to the FC ([10], [11], [8]).

To ensure the dynamic exchange of energy between the FC source, the load and the SC modules, various converter topologies and their control are presented ([12], [13]). The general system topology is represented in Fig. 1 which is usually called hybrid energy storage system (HESS).

The control of the HESS has been studied by using conventional linear control techniques (see e.g. [14], [15], [16], [17], [18], [19]). However both the dc-dc converters and the fuel cell exhibit a highly nonlinear behavior [20], so that linear control only can ensure stability for a certain operation point. In this paper the modeling and the nonlinear control strategy for a hybrid energy storage system is investigated.

The paper is organized as follows: in Section 2, the HESS in electric vehicle is described; Sections 3 is devoted to the system modeling; controller design and closed-loop analysis is presented in Section 4; the controller performances are illustrated by numerical simulation in Section 5; Section 6 provides a conclusion of the paper.

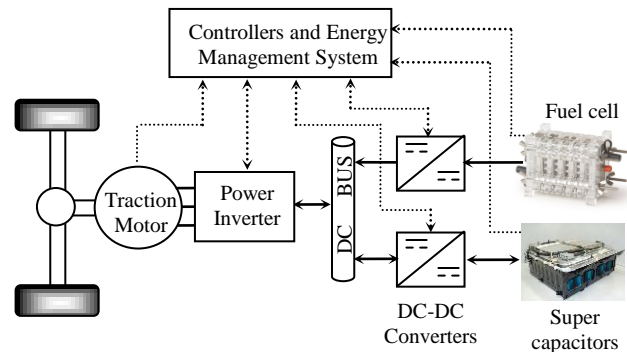


Fig.1: Power circuit of typical hybrid vehicle

## II. PRESENTATION OF ELECTRIC CIRCUIT STRUCTURE

Figure 2 shows the studied hybrid energy storage system (HESS) of the electric vehicle. It consists of a 400-V dc link supplied by a 27kW PEMFC used as the main source, through a current nonreversible dc/dc converter, a SC bank used as an auxiliary source and which is connected to the dc link through a current reversible dc/dc converter, and the load represented by the inverter driving the electric motor.

The function of the FC is to supply mean power to the load,

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whereas the SC is used as a power source: it supplies transient power demand, and peak loads required during acceleration and deceleration.

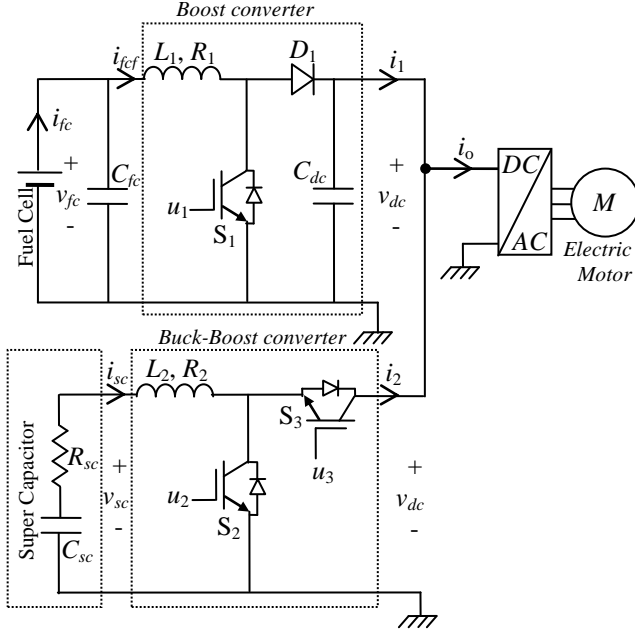


Fig.2: Fuel cell supercapacitor hybrid energy storage system

#### A. FC converter (boost)

As the main source FC is not current reversible the boost power is used to adapt the low dc voltage delivered by the FC at rated power of dc bus [14]. Thus, it is composed of a high frequency inductor  $L_1$ , an output filtering capacitor  $C_{dc}$ , a diode  $D_1$  and a main switch, insulated-gate bipolar transistor (IGBT),  $S_1$  controlled by a binary input signal  $u_1$ . The input capacitor  $C_{fc}$  is used to protect the FC against overvoltage in transient high power demand of the load.

#### B. SC converter (buck-boost)

The SC is connected to the dc bus by means of a two-quadrant dc/dc converter, also called buck-boost converter. Supercapacitor current, which flows across the storage device, can be positive or negative, allowing energy to be transferred in both directions.  $L_2$  represents the inductor used for energy transfer and filtering. The inductor size is classically defined by switching frequency and current ripple [21]. The converter is driven by means of binary input signals  $u_2$  and  $u_3$  applied on the gates of the two IGBTs  $S_2$  and  $S_3$ , respectively.

#### C. Energy management strategy of hybrid power source

The main energy management strategy for the combined system reported in many places ([21], [22], [23], [24]). To realize the energy-management strategy the dc-dc power converters has to be properly controlled. Accordingly, the boost converter is driven to realize a classical dc bus voltage regulation. The buck-boost converter is driven so that the SC current  $i_{sc}$  perfectly tracks its reference  $i_{scref}$  which is generated by the energy management system. The generation of current

reference  $i_{scref}$  is not treated in this work as the focus is made on the power converters non linear controller design. However, this current is positive in discharging mode and negative in charging mode [14].

### III. HYBRID ENERGY STORAGE SYSTEM MODELING

#### A. Energy sources models

The classical static V-I polarization for a fuel cell is known to be nonlinear [25]. The voltage reduction is caused by three major losses: activation losses, ohmic losses, and transport losses.

The Supercapacitor can be represented by its classical equivalent circuit consisting of a capacitance ( $C_{sc}$ ), an equivalent series resistance (ESR,  $R_{sc}$ ) representing the charging and discharging resistance and an equivalent parallel resistance (EPR) representing the self discharging losses ([26], [27]).

#### B. Boost converter modeling

From Fig. 2 one can obtain the power stage bilinear equations, considering some non-idealities. For instance, the inductances  $L_1$  and  $L_2$  shown in Fig.2 present an equivalent series resistance (ESR),  $R_1$  and  $R_2$ , respectively. Each IGBT switch is controlled by using a PWM signal  $u_j$  ( $j=1,2,3$ ) which takes values from the subset  $\{0, 1\}$ .

From inspection of the circuit, shown in Fig.2, and taking into account that  $u_1$  can take the binary values 1 or 0, the following bilinear switching model can be obtained:

$$\frac{di_{fcf}}{dt} = -(1-u_1) \frac{v_{dc}}{L_1} - \frac{R_1}{L_1} i_{fcf} + \frac{v_{fc}}{L_1} \quad (1a)$$

$$\frac{dv_{dc}}{dt} = (1-u_1) \frac{i_{fcf}}{C_{dc}} - \frac{1}{C_{dc}} i_1 \quad (1b)$$

where  $i_{fcf}$  and  $i_1$  being, respectively, the inductor input current and the output current of the boost converter;  $v_{fc}$  the FC voltage;  $v_{dc}$  the dc bus voltage.

#### C. Buck-Boost converter modeling

This converter can operate as a boost converter or a buck converter. Indeed, in discharging mode of the SC ( $i_{sc} > 0$ ) the converter operates as a boost converter, however, in charging mode of SC ( $i_{sc} < 0$ ) it operates as a buck converter. As our goal is to enforce the SC current  $i_{sc}$  to track its reference  $i_{scref}$  provided by the energy management system, one can define a binary variable  $k$  as follows:

$$k = \begin{cases} 1 & \text{if } i_{scref} > 0 \quad (\text{Boost mode}) \\ 0 & \text{if } i_{scref} < 0 \quad (\text{Buck mode}) \end{cases} \quad (2)$$

##### 1) Boost mode operation ( $k=1$ )

In this case the control input signal  $u_3$  is fixed to zero ( $u_3=0$ ) and  $u_2$  is a PWM variable input. From inspection of the circuit, shown in Fig.2, and taking into account that  $u_2$  can take the binary values 1 or 0, the following bilinear switching model can be obtained:

$$\frac{di_{sc}}{dt} = -(1-u_2)\frac{v_{dc}}{L_2} - \frac{R_2}{L_2}i_{sc} + \frac{v_{sc}}{L_2} \quad (3a)$$

$$i_2 = (1-u_2)i_{sc} \quad (3b)$$

where  $i_{sc}$  being the SC current.

## 2) Buck mode ( $k=0$ )

The control input signal  $u_2$  is fixed to zero ( $u_2=0$ ) and  $u_3$  acts as the PWM variable input. Also, from Fig. 2, and taking into account that  $u_3 \in \{0, 1\}$ , the following model can be obtained

$$\frac{di_{sc}}{dt} = -u_3\frac{v_{dc}}{L_2} - \frac{R_2}{L_2}i_{sc} + \frac{v_{sc}}{L_2} \quad (4a)$$

$$i_2 = u_3i_{sc} \quad (4b)$$

## D. Global system model

On the basis of the previous three partial models ((1), (3) and (4)), the aim now is to obtain a global model of the system useful for control design purpose. From the inspection of (3) and (4) one can readily obtain the following buck boost converter global model:

$$\frac{di_{sc}}{dt} = -[k(1-u_2) + (1-k)u_3]\frac{v_{dc}}{L_2} - \frac{R_2}{L_2}i_{sc} + \frac{v_{sc}}{L_2} \quad (5a)$$

$$i_2 = [k(1-u_2) + (1-k)u_3]i_{sc} \quad (5b)$$

In the other hand, from Fig.2 and taking into account (5b) one obtains:

$$i_1 = i_o - i_2 = i_o - [k(1-u_2) + (1-k)u_3]i_{sc} \quad (6)$$

where  $i_o$  being the load current.

Finally, using ((1), (5a) and (6) the following bilinear switched model of the global system is obtained:

$$\frac{di_{fcf}}{dt} = -(1-u_1)\frac{v_{dc}}{L_1} - \frac{R_1}{L_1}i_{fcf} + \frac{v_{fc}}{L_1} \quad (7a)$$

$$\frac{di_{sc}}{dt} = -u_{23}\frac{v_{dc}}{L_2} - \frac{R_2}{L_2}i_{sc} + \frac{v_{sc}}{L_2} \quad (7b)$$

$$\frac{dv_{dc}}{dt} = (1-u_1)\frac{i_{fcf}}{C_{dc}} + u_{23}\frac{i_{sc}}{C_{dc}} - \frac{i_o}{C_{dc}} \quad (7c)$$

Where  $u_{23}$  is the only control input variable of the buck-boost converter defined as follows:

$$u_{23} = k(1-u_2) + (1-k)u_3 \quad (8)$$

The generation of effective control input signals  $u_2$  and  $u_3$  from  $u_{23}$  will be investigated later in this paper.

For control design purpose, it is more convenient to consider the following averaged model, obtained by averaging the model (7) over one switching period

$$\frac{dx_1}{dt} = -(1-\mu_1)\frac{x_3}{L_1} - \frac{R_1}{L_1}x_1 + \frac{v_{fc}}{L_1} \quad (9a)$$

$$\frac{dx_2}{dt} = -\mu_{23}\frac{x_3}{L_2} - \frac{R_2}{L_2}x_2 + \frac{v_{sc}}{L_2} \quad (9b)$$

$$\frac{dx_3}{dt} = (1-\mu_1)\frac{x_1}{C_{dc}} + \mu_{23}\frac{x_2}{C_{dc}} - \frac{i_o}{C_{dc}} \quad (9c)$$

being  $x_1$  the average value of the current  $i_{fcf}$  ( $x_1 \triangleq i_{fcf}$ ),  $x_2$

is the average value of the SC current ( $x_2 \triangleq i_{sc}$ ),  $x_3$  is the average value of the dc bus voltage  $v_{dc}$  ( $x_3 \triangleq v_{dc}$ ),  $\mu_1$  and  $\mu_{23}$  are the duty cycle, i.e. average values of the binary control inputs  $u_1$  and  $u_{23}$  ( $\mu_1 \triangleq u_1$ ,  $\mu_{23} \triangleq u_{23}$ ), respectively, which take values in  $[0,1]$ .

Notice that the nonlinear model (9) is a multi-input multi-output (MIMO) system, which can be difficult to control by using classical linear control theory. Now, we are ready to elaborate an appropriate control law that can fulfill all the above mentioned requirements.

## IV. CONTROLLER DESIGN AND ANALYSIS

### A. Control objectives

In order to define the control strategy, first one has to establish the control objectives, which can be formulated as following:

- i) tight dc bus voltage regulation under load variations,
- ii) perfect tracking of SC current  $i_{sc}$  to its reference  $i_{scref}$ ,
- iii) and asymptotic stability of the whole system.

### B. Nonlinear control design

The first control objective is to enforce the dc bus voltage  $v_{dc}$  to track a given constant reference signal  $V_{dcref}$  [30].

However, it is well known that the boost converter has a non-minimum phase feature ([28], [29]). Such an issue is generally dealt with by resorting an indirect design strategy. More specifically, the objective is to enforce the input inductor current  $i_{fcf}$  to track a reference signal, say  $I_{fcfref}$ . The latter is chosen so that if (in steady state)  $i_{fcf} = I_{fcfref}$  then

$v_{dc} = V_{dcref}$ , where  $V_{dcref} > v_{fc}$ . It follows from power conservation consideration, also called PIPO (Power Input equals Power Output), that  $I_{fcfref}$  is related to  $V_{dcref}$  by the relationship

$$I_{fcfref} = \lambda \left( \frac{V_{dcref}i_o - v_{sc}I_{scref}}{v_{fc}} \right) \quad (10)$$

where  $\lambda \geq 1$  being an ideality factor introduced to take into account all losses: switching losses in the converters and the losses in the inductances ESR  $R_1$  and  $R_2$ .

In order to carry out the first control objective, the following error is introduced

$$e_1 = x_1 - I_{fcfref} \quad (11)$$

Achieving the dc bus voltage regulation objective amounts to enforcing the error  $e_1$  to vanish. To this end, the dynamic of  $e_1$  have to be clearly defined. Deriving (11), it follows from (9a) that:

$$\dot{e}_1 = -(1-\mu_1)\frac{x_3}{L_1} - \frac{R_1}{L_1}x_1 + \frac{v_{fc}}{L_1} - I_{fcfref} \quad (12)$$

The goal, now, is to make  $e_1$  exponentially vanishing by enforcing  $\dot{e}_1$  to behave as follows

$$\dot{e}_1 = -c_1e_1 + e_3 \quad (13)$$

where  $c_1 > 0$  being a design parameter, and

$$e_3 = x_3 - x_{3d} \quad (14)$$

is the error between the dc bus voltage  $x_3$  and its desired value  $x_{3d}$ . The desired value  $x_{3d}$  will be specified later.

Combining (12) and (13) the control law of boost converter input signal is obtained,

$$\mu_1 = 1 - \frac{L_1}{x_3} \left\{ c_1 e_1 - e_3 + \frac{v_{fc} - R_1 x_1}{L_1} - \dot{i}_{fc \text{ref}} \right\} \quad (15)$$

In (15) the term  $e_3$  is a damping term introduced in the control law to adjust the output response. Its dynamic will be investigated later.

The next step is to elaborate a control law of buck-boost converter input signal  $\mu_{23}$ , bearing in mind the second control objective. To this end, the following error is introduced

$$e_2 = x_2 - I_{sc \text{ref}} \quad (16)$$

Its derivative, using (9b), is

$$\dot{e}_2 = -\mu_{23} \frac{x_3}{L_2} - \frac{R_2}{L_2} x_2 + \frac{v_{sc}}{L_2} - \dot{I}_{sc \text{ref}} \quad (17)$$

In order to achieve the tracking objective of the SC current  $i_{sc}$ , one can seek that the error  $e_2$  vanish exponentially. This amounts to enforcing its derivative  $\dot{e}_2$  to take the following form

$$\dot{e}_2 = -c_2 e_2 \quad (18)$$

where  $c_2 > 0$  being a design parameter. Finally, from (16) and (18), the control law  $\mu_{23}$  can be easily obtained as follows

$$\mu_{23} = \frac{L_2}{x_3} \left\{ c_2 e_2 + \frac{v_{sc} - R_2 x_2}{L_2} - \dot{I}_{sc \text{ref}} \right\} \quad (19)$$

Since the two controls laws  $\mu_1$  and  $\mu_{23}$  are clearly defined, the concern is now to check that the stability of the closed loop is perfectly ensured. This will be done in the next subsection.

### C. Stability analysis

The third control objective can now be analyzed. This can be carried out by checking that the elaborated controllers (15) and (19) stabilize the whole system with the state vector  $(e_1, e_2, e_3)$ . To this end the following quadratic Lyapunov function is considered

$$V = \frac{1}{2} e_1^2 + \frac{1}{2} e_2^2 + \frac{1}{2} e_3^2 \quad (20)$$

The aim is to make the derivative of  $V$ ,  $\dot{V}$ , negative definite. Thus,  $\dot{V}$  is obtained from (20) using (13) and (18), which yields to

$$\dot{V} = -c_1 e_1^2 - c_2 e_2^2 + e_3(e_1 + \dot{e}_3) \quad (21)$$

This suggest choosing the derivative  $\dot{e}_3$  as follows

$$\dot{e}_3 = -c_3 e_3 - e_1 \quad (22)$$

where  $c_3 > 0$  being a design parameter. Indeed, with this choice, the derivative  $\dot{V}$  of the Lypunov function can simply

rewritten as follows

$$\dot{V} = -c_1 e_1^2 - c_2 e_2^2 - c_3 e_3^2 \quad (23)$$

which means that  $\dot{V} \leq 0$  and in turn shows that the closed loop system with the state vector  $(e_1, e_2, e_3)$  is globally asymptotically stable (GAS).

Finally, to achieve the control design one needs the expression of the desired value  $x_{3d}$  of dc bus voltage  $x_3$  which is used in the control law (15). Its dynamic can be easily obtained from (22), using (14) and (9c), as follows

$$\dot{x}_{3d} = \frac{1}{C_{dc}} [(1 - \mu_1)x_1 + \mu_{23}x_2 - i_o] + c_3 e_3 + e_1 \quad (24)$$

or equivalently

$$x_{3d} = \frac{1}{s} \left\{ \frac{1}{C_{dc}} [(1 - \mu_1)x_1 + \mu_{23}x_2 - i_o] + c_3 e_3 + e_1 \right\} \quad (25)$$

where  $s$  is Laplace operator.

The main results of the paper are now summarized in the following theorem.

**Theorem.** Consider the closed-loop system consisting of the fuel cell supercapacitor hybrid energy storage system represented by (7a-c), and the controller composed of the control laws (15) and (19). Then, one has:

- i) The closed loop system is GAS.
- ii) The error  $e_1$  converge to zero implying tight dc bus voltage regulation.
- iii) The error  $e_2$  converge to zero implying perfect tracking of SC current  $i_{sc}$  to its reference  $i_{sc \text{ref}}$ .  $\square$

## V. SIMULATION RESULTS

The performances of the proposed nonlinear controller are now illustrated by simulation. The controlled system characteristics are listed in Table 1. The PEMFC is with the following characteristics: 262V, 80A, 27kW.

The simulation bench of the hybrid energy storage system control is described by Fig. 5 and is simulated using the MATLAB software. Fig.5 shows the circuit that generates buck-boost converter binary input signals  $u_2$  and  $u_3$  form the control law  $\mu_{23}$  and  $i_{sc \text{ref}}$  according the equations (2) and (8).

The design control parameters are chosen as follows, which proved to be convenient:  $c_1 = 10 \times 10^3$ ,  $c_2 = 2 \times 10^3$  and  $c_3 = 10^2$ . The resulting control performances are shown by Figs 5 to 9.

TABLE 2: PARAMETERS OF THE CONTROLLED SYSTEM

| Parameter                            | Value  |
|--------------------------------------|--------|
| Inductance $L_1$ and $L_2$           | 3.3mH  |
| Inductances ESR, $R_1$ and $R_2$     | 20mΩ   |
| DC bus Filtering capacitor, $C_{dc}$ | 1.66mF |
| Boost input capacitor, $C_{fc}$      | 1.66mF |
| Supercapacitor, $C_{sc}$             | 21.27F |

|                              |              |
|------------------------------|--------------|
| Supercapacitor ESR, $R_{sc}$ | 66m $\Omega$ |
| Switching frequency, $f_s$   | 15kHz        |

Figure 5 and Fig.6 describe the controller performances in presence of a constant reference  $I_{scref} = 10A$  and successive load current  $i_o$  jumps. The jumps occur between 50A and 20A; and between 20A and 70A. It is seen that the control performances are satisfactory, despite the load current variations. Indeed, Fig.5 shows that the dc voltage  $v_{dc}$  is regulated to its desired value  $V_{dcref} = 400V$ ; Fig.6 illustrates the control signals  $\mu_1$  and  $\mu_{23}$ . Figures 7 to 9 describe the controller performances in presence of a constant current load  $i_o = 40A$  and successive variations of SC current reference  $I_{scref}$ . The variations are performed with jumps between 20A and -30A; and between -30A and 10A. Also, the figures show that the control behavior is satisfactory. Indeed, in Fig. 7 one can shows that the dc voltage  $v_{dc}$  is perfectly regulated to its desired value  $V_{dcref} = 400V$ ; Fig.8 illustrates that the SC current  $i_{sc}$  tracks its reference signal  $I_{scref}$ ; finally, Fig.9 illustrates the control signals  $\mu_1$  and  $\mu_{23}$ .

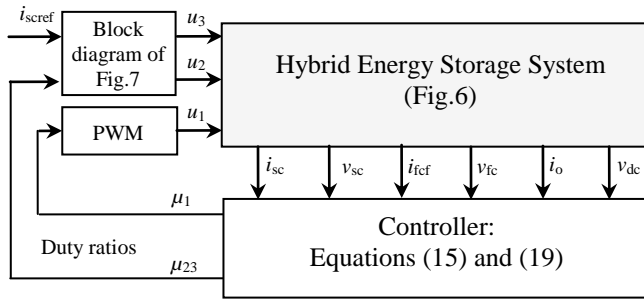


Fig.3: Simulation bench for HESS control

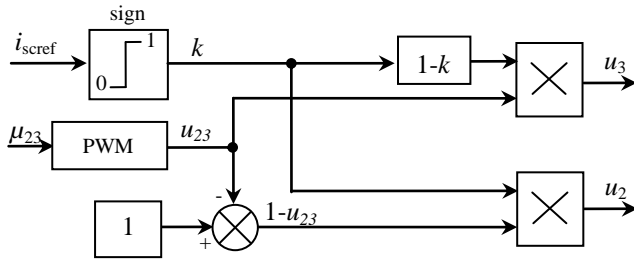


Fig.4: Block diagram of input signals  $u_2$  and  $u_3$  generation

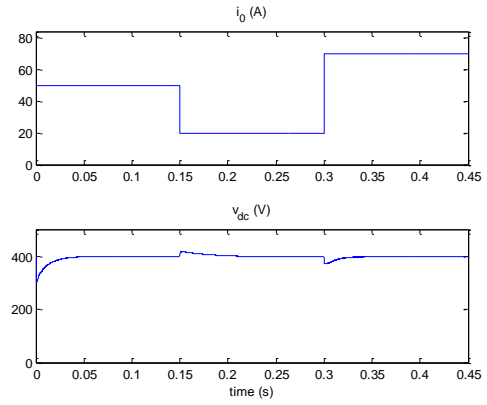


Fig.5: The dc voltage in presence of load current jumps

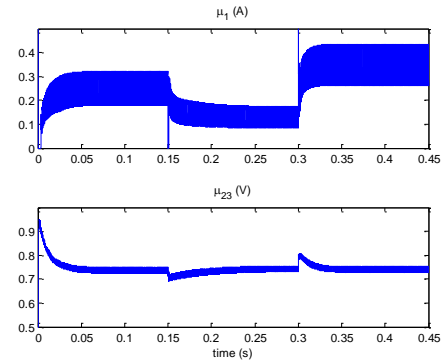


Fig.6: The control signals in presence of load current jumps

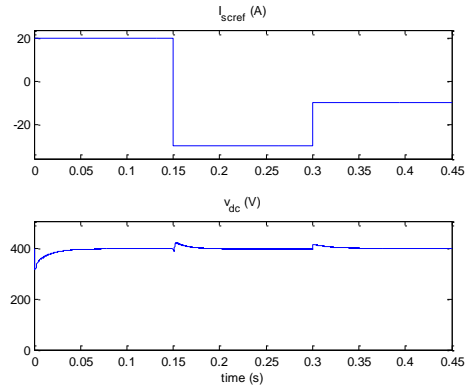


Fig.7: The dc voltage in presence of SC current reference jumps

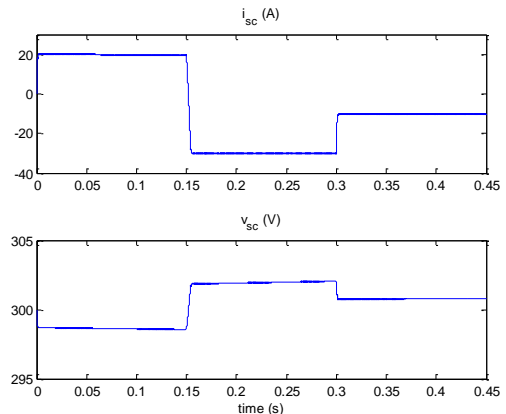


Fig.8: The SC signals in presence of SC current reference jumps

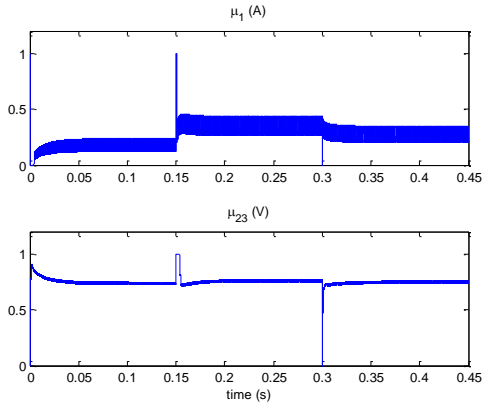


Fig.9: The control signals in presence of SC current reference jumps

## VI. CONCLUSION

The problem of controlling a hybrid energy storage system used in electric vehicle has been considered. The system consists on fuel cell main source and a supercapacitor auxiliary source. In order to manage the energy conversion between sources and load, two dc-dc power converters has been used. The aim is to elaborate an adequate controller that generates the binary power converters input signals in order to satisfy the following requirements: i) tight dc voltage regulation, ii) perfect tracking of supercapacitor current to its reference and, iii) asymptotic stability of the closed loop system. The controller is obtained from the nonlinear averaged model (9) using a Lyapunov based theory. Using both formal analysis and simulation, it has been proven that the obtained controller achieves the performances for which it was designed.

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